Name: $\qquad$
Date: $\qquad$

## Discrete Probability Distributions Worksheet

1. You flip four coins. Let $X$, the random variable, be the number of heads on all four coins.
a. List the sample space for the experiment. (all possible outcomes)
b. What are the possible values for $x$ ? (how many heads can land)
c. Is the random variable, $x$, continuous or discrete?
d. Construct a probability distribution for this experiment.

## X


$P(X)$
e. Construct a histogram for the probability distribution in the space below.
2. Determine if the following are probability distributions (if no, state why).
$\begin{array}{llllll}\text { a. } X & 3 & 6 & 9 & 12 & 15 \\ P(X) & 4 / 9 & 2 / 9 & 1 / 9 & 1 / 9 & 1 / 9\end{array}$
$\begin{array}{llllll}\text { b. } X & 1 & 2 & 3 & 4 & 5 \\ P(X) & 3 / 10 & 1 / 10 & 1 / 10 & 2 / 10 & 3 / 10\end{array}$
$\begin{array}{lllll}\text { c. } X \quad & 20 & 30 & 40 & 50\end{array}$
$\begin{array}{lllll}P(X) & 1.1 & 0.2 & 0.9 & 0.3\end{array}$

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3. Construct a probability distribution for the data and draw a histogram for the following:
a. The probabilities that a patient will have 0,12 , or 3 medical tests performed on entering a hospital are $6 / 15,5 / 15,3 / 15$, and $1 / 15$ respectively.

## x

$\qquad$
$P(X)$
b. A die is loaded in such a way that the probabilities of getting $1,2,3,4,5$, and 6 are $1 / 2,1 / 6$, $1 / 12,1 / 12,1 / 12$, and $1 / 12$ respectively.

X
$\qquad$
$P(X)$
c. A box contains $3 \$ 1$ bills, $2 \$ 5$ bills, $1 \$ 10$ bill, and $1 \$ 20$ bill.

## x

$P(X)$
d. A family has three children. Let $X$ represent the number of boys. * order doesn't matter*

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X
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$P(X)$

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4. Below is a probability distribution for the number of math failures of $B C$ students. $(X=$ students who have failed)

| $X$ | 0 | 1 | 2 | 3 | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $P(X)$ | .41 | .38 |  | .08 | .02 |

a. $\quad P(X=2)$
b. $P(X<2)$
c. $P(X \leq 2)$
d. $P(X \leq 1)$
e. $P(X>2)$
f. $P(X=3$ or $X=4)$

Name:

## Games \& Expectation

1. A box contains ten $\$ 1$ bills, five $\$ 2$ bills, three $\$ 5$ bills, one $\$ 10$ bill, and one $\$ 100$ bill. A person is charged $\$ 20$ to select one bill. Find the expected value for this game. Is this game fair?
2. If a person rolls doubles when he tosses two dice, he wins $\$ 5$. The cost to play the game is $\$ 1$. Is this game fair?
3. A raffle sells 100 tickets at $\$ 5$ a piece. There is one $\$ 500$ prize, five $\$ 100$ prizes, and ten $\$ 50$ prizes. What is the expected value? Hint: Find the $P$ (You win) and $V$ (You win) along with the P(You lose) and V(You lose).
