

## 5.4 Indirect Proof

G.T.4 Indirect Proof

Indirect Proof \_\_\_\_\_

**Step One:** Identify the conclusion you are asked to prove. Make the assumption that this conclusion is false by assuming that the opposite is true.

**Example 1:** State the assumption necessary to start an indirect proof of each statement.

- $m\angle ABC < m\angle CBA$
- $\triangle DEF \cong \triangle RST$
- Line  $a$  is perpendicular to line  $b$ .
- $\angle 5$  is supplementary to  $\angle 6$ .

**Step Two:** Use logical reasoning to show that this assumption leads to a contradiction of the hypothesis, or some other fact, such as a definition, postulate or corollary.

**Step Three:** Point out that since the assumption leads to a contradiction, the original conclusion, what you were asked to prove, must be true.

**Example 2:** Write an indirect proof to show that if  $-2x + 11 < 7$  then  $x > 2$

**Assumption:**

**Contradiction:**

**Therefore:**

**Example 3:** Given :  $x + 2$  is an even integer.

Prove :  $x$  is an even integer

Assumption:

Contradiction:

Therefore:

**Example 4:** Given :  $xy$  is an odd integer

Prove :  $x$  and  $y$  are both odd integers

Assumption:

Contradiction:

Therefore:

**Example 5:** Given : A triangle can have only one right angle

Assumption:

Contradiction:

Therefore: